Algorithmic patterns Data Structures and Algorithms for Comnal Linguistics III (ISCL-BA-07) Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de

Winter Semester 2024/25

## Recursion

Your task from the first lecture: writing a recursive linear search the complete code

- Recursion is relatively easy: if val -- meq[0]:
   return i
  else:
   return rl\_mearch(meq[::], val, i-:)
- . And we need a base case: if not meg: # onp
- the compete come

  | def rl search(seq, val, i=0):
  | if not seq:
  | return None
  | if val = seq[0]:
  | return rl, search(seq[::], val, i=1)
  | return rl, search(seq[::], val, i=1) Can we improve this?

Recursion: practical issues ration depth :

- Each function call requires some bookkeeping
   Compilers/interpreters allocate space on a stack for the bookkeeping for each function call
- Most environments limit the number of recursive calls: long chains of recursion are likely to be caused by programming errors
- . Tail recursion (e.g., our recursive search example) is easy to convert to iteration
- It is also easy to optimize, and optimized by many compilers (not by the Python interpreter)

Visualizing binary recursion

Brute force

- rate all possible cases (e.g., to find the
- best solution) Common in combinatorial problems
- Often intractable, practical only for small input sizes
- It is also typically the beginning of finding a more efficient approach

Segmentation

| def segment\_r(seq): | segs = (] = : | if 1 term ([seq]) = : | for seq in segment\_r(seq[::]): | for seq in segment\_r(seq[::]): | segs\_append([seq[0]] + seg[0]] + seg[::]) | return\_seq

. Can you think of a non-recursive solution:

Overview

- - Revisiting recursion
     Brute force
     Divide and conque
     Greedy algorithms

How does this recursion work



Another recursive example every algorithm course is required to

Fibonacci numbers are defined as Fo = 0

 $F_1 = 1$  $F_n = F_{n-1} + F_{n-2} \quad \text{for} \quad n > 1$ 

- · Recursion is common in math, and maps well to the recursive algorithms
  - - recursion, each function call creates two calls to self . We follow the math exactly, but is this code officiant?

: def fib(n): : if n <= 1: : return n : return fib(n-2) + fib(n-1)

Complexity of (naive) Fibonacci algorithm recursion tree for fib(7)

Brute force

- · Segmentation is prevalent in CL
- eggmentation is prevaited in CL.

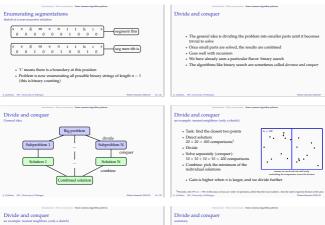
  Examples include finding words: tokenization (particularly for writing sy
  that do not use within space)

  Finding sub-rood units (e.g., morphemes, or more specialized applicatio
  compound splitting)

  Psycholinguistics: how do people extract words from continuous speech?
- We consider the following problem:
  Given a metric or score to determine the "best" segmentation
  We enumerate all possible ways to segment, pick the one with the best score
- . How can we enumerate all possible segmentations of a string?

Segmentation

[[abcd], [abc, d], [ab, cd], [ab, c, d], [a, bcd], [a, bc, d], [a, b, cd], [a, b, c, d]] [[bcd], [bc, d], [b, cd], [b, c, d]]



- Task: find the closest two portions Direct solution:
  20 × 20 = 400 comparisons<sup>3</sup>

- Divide
- \* Solve separately (conquer):  $10 \times 10 + 10 \times 10 = 200$  comparisons
- Combine: pick the minimum of the individual solutions
- Gain is higher when n is larger, and we di

### Greedy algorithms

- · An algorithm is greedy if it optimizes a local co
  - . For some problems, greedy algorithms result in cor
  - . In others they may result in 'good enough' solutions
  - . If they work, they are efficient
  - An important class of graph algorithms fall into this category (e.g., finding shortest paths, scheduling)

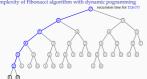


# Dynamic programming

- . Dynamic programming is a method to save earlier results to reduce computation
- . It is sometimes called memoization (it is not a typo)

- Again, a large number of algorithms we use fall into this category, including common parsing algorithms

# Complexity of Fibonacci algorithm with dynamic pogramming recursion tree for fib(



- . This is probably the most common pattern
- . Divide and conquer does not always yield good results, the cost of merging
- should be less than the gain from the division(s) Many of the important algorithms fall into this category:

  - menge seet and quick sort (coming soon)
     integer multiplication
     matrix multiplication
     fast Fourier transform (FFT)

### Greedy algorithms 'change making

## · We want to produce minimum number of coins for a particular sum s

- Pick the largest coin c <= s</li>
- 2. set s = s c 3. repeat 1 & 2 until s = 0
- Is this algorithm correct?
- $\star$  Think about coins of 10, 30, 40 and apply the algorithm for the sum value of 60 . Is it correct if the coin values were limited Euro coins?

Dynamic programming

### wie Fib : def memofib(n, memo = {0: 0, 1:1}):

if n not in memo:
 memo[n] = memofib(n-1) + memofib(n-2)
return memo[n]

- . We save the results calculated in a dictionary,
- if the result is already in the dictionary, we return without recursion
- . Otherwise we calculate recursively as before
- The difference is big, but there is also a 'neater' solution without (explicit)
- memoization

# Summary

### We saw a few general appro ient) ale

- Designing algorithms is not a mechanical procedure: It requires creativity
   There are other common patterns, including
   Backtracking, Branch-and-bound
- Randomized algorithms
   Distributed algorithms (sometime called swarm optimization)
- Designing algorithm ns is difficult (possibly, not as difficult as analyzing them)
- \* Reading: Goodrich, Tamassia, and Goldwasser (2013, chapter 12)

Introduction. More on recursion. Some common algorithm patterns.	Introduction Marcon recorder. Some common algorithm patterns
Nearest neighbors an exercise	Linear search a little bet of optimization
<ul> <li>Dolins and implement a divide and conspor algorithm for neuron neighbor problem, which divides the input into two until the solution becomes trivial.</li> <li>Analyse your algorithm and compare to the naive version sketched above (an implementation was provided in the previous lecture).</li> </ul>	def () constitue, val., v();   def () constitue, val., va
	Which one is faster, and why?
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Better solutions for Fibonacci numbers	Segmentation with yield
def finish(n)     def finish(n)       def finish(n)       def finish(n)       def finish(n)	def segment r(seq):   if les(seq) == 1:   plain (seq) == 1:   all plain (seq) == 1:   for seq in segment r(seq[i:]):   for seq in segment r(seq[i:]):   yield (seq[i]) = seq[i] = seq[i:]
Which one is faster/better?	yield [seq[0] + seg[0]] + seg[i:]
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