Graph Traversal nal Linguistics III

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Graph traversal * A graph traversal is a systematic way to visit all nodes in a graph

- Graph traversal is one of the basic tasks on a graph, answering many interesting questions

- Is there a path from one node to another?

 What is the shortest path (with minimum number of edges) between the path connected?

 Is the graph connected?

 Is the graph cyclic?

- Two main methods of traversals are breadth-first and depth-first

DFS - intuition

- · Depth first search follows the same idea as exploring a labyrinth with a string and a chalk
- Visit each intersection (node), while marking the path you took with the string
- Mark each visited node, backtrack (following the string) when hit a dead end



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DFS - algorithm

· Depth-first search (DFS) is easy with def dfs(start, visited=Nome):
 if visited is Nome:
 visited = {tart: Nome}
 for node in start.neighbors():
 if node not in visited:
 visited[node] = start

· DFS starts from a start node

· Marks each node it visits as visited (typically

nut it in a set data structure) . Then take an arbitrary sumisited neighbor

leads to the start node with no unvisited

and continue visiting the nodes reco · Algorithm terminates when backtracking

nodes left

DFS - demonstration, definitions



. The edges that we take to discover a new node are called the discovery edges * The discovery edges form the DFS tree

. The other edges are called non-tree edges . The edges to an ancestor in the DFS tree are called back

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Properties of DFS

· DFS visits all nodes in the con-

- cted comp
- Discovery edges form a spanning tree of the connected component
- If a node v is connected to the start node, there is a path from the start node v
 in the DFS tree . The DFS algorithm visits each node and checks each edge once (twice for
- undirected graphs
- \bullet The complexity of the algorithm is O(n+m) for n nodes and m edges

BFS - intuition

- · A way to think about breadth-first search (BFS) is to explore all options in parallel
- . In the maze, at every intersection
- send out people in all directions BFS divides the nodes into levels:
 - starting node at level 0
 nodes directly accessible
 at level 1



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BFS - algorithm

- def bfs(start):
 queue = [start]
 visited = {start: None}
- visited = (start: Bone)
 while queue:
 current = queue.pop(0)
 for node in current neighbors():
 if node not in visited:
 visited[node] = current
 queue.append(node)
- · Typically BFS is implemented with a queue
- The algorithm visits nodes closest to the start node first
- . If you replace the queue with a stack, you get an iterative version of the DFS

BFS - demonstration



- · Similar to DPS, the edges that we take to discover a new node are called the discov edges
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Properties of BFS

· DFS visits all nodes in the connected component from the start node

- Discovery edges form a spanning tree of the connected component
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- the start node to v . The BFS algorithm visits each node and checks each edge once
- * The complexity of the algorithm is O(n + m) for n nodes and m edges

- · Finding a path bet veen two n des (if one exists)
- Testing whether G is connected

Some other problems solved by graph traversal

Find the connected components

· Is the graph cyclic?

Computing connected components of G

Problems solved by graph traversals

- Detecting cycles

Finding a path between two nodes

- Traverse the graph from the source node, record the discovery edges · Start from the target node, trace the path back to the
- · With BFS, we get the
- shortest path * Running time is the length of the path: O(n)
- def find_path(source, target, visited):
 path = []
 if target in visited:
 path.append(target)
 current = target
 while current is not source:
 parent = visited(current)

 - path.append(parent) current = parent return path.reverse()
- A directed graph is cyclic if there is a back edge during graph tra A undirected graph is cyclic if a traversal finds any visited nodes (if there are back, forward or cross edges)

Is the graph connected?
 Yes if the "visited" nodes have the same length as the nodes of the graph.

- Run traversal multiple times, until all nodes are visited

Summary	Acknowledgments, credits, references
Traversal is one of the basic operations in graphs Graph traversals already solve some interesting problems: Find a goal (chores) with 1875 Find a goal (chores) with 1875 Find cycles Redding on graphs: Coodrich, Tramssta, and Goldwasser (2013, chapter 14) Not: More graph algorithms: special problems on directed graphs, shortest paths	■ Goodrich, Michael T., Roberto Tamassia, and Michael H. Goldwasser (2013). Data Structures and Algorithms in Python. John Wiley & Sons, Incorporated. sase: 9701118470734.
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